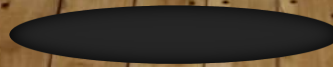


HIGGS BOSON: A PORTAL TO NEW PHYSICS

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September 21-25, 2026



Drei Generationen der Materie (Fermionen)				
	I	II	III	
Masse	2,3 MeV	1,275 GeV	173,07 GeV	125,9 GeV
Ladung	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0
Spin	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	0
Name	u up	c charm	t top	H Higgs Boson
Quarks	4,8 MeV $-\frac{1}{3}$ $\frac{1}{2}$ d down	95 MeV $-\frac{1}{3}$ $\frac{1}{2}$ s strange	4,18 GeV $-\frac{1}{3}$ $\frac{1}{2}$ b bottom	0 0 1 g Gluon
	<2 eV 0 $\frac{1}{2}$ ν_e Elektron-Neutrino	<0,19 MeV 0 $\frac{1}{2}$ ν_μ Myon-Neutrino	<18.2 MeV 0 $\frac{1}{2}$ ν_τ Tau-Neutrino	91,2 GeV 0 1 Z ⁰ Z Boson
	0,511 MeV -1 $\frac{1}{2}$ e Elektron	105,7 MeV -1 $\frac{1}{2}$ μ Myon	1,777 GeV -1 $\frac{1}{2}$ τ Tau	80,4 GeV ± 1 1 W [±] W Boson
Leptonen				Eichbosonen

STANDARD MODEL OF PARTICLE PHYSICS

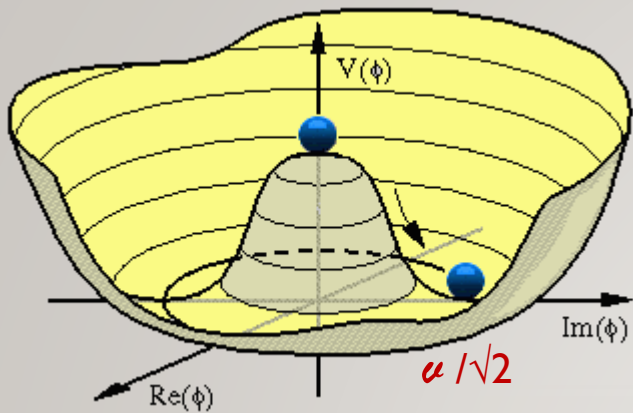
1. Describes elementary particles and their interactions
2. 'Equations of motion' in classical physics are substituted with the Lagrangian (particles are quantum and relativistic)
3. Interactions are consequence of symmetries (of the Lagrangian) to the local phase transformations giving rise to vector bosons (gauge symmetries)
4. Higgs mechanism: Assumption that there is a scalar field, with a ground state (vacuum ω) that does not have the symmetries of the Lagrangian (spontaneous symmetry breaking)
5. Interaction with the scalar field (Higgs) introduces mass terms in the Lagrangian

$$\mathcal{L}_{\text{SM}} = \mathcal{L}_{\gamma ff} = -eQ_f \bar{f} \gamma^\mu f A_\mu + \mathcal{L}_{W ff'} = -\frac{g}{\sqrt{2}} (\bar{f} \gamma^\mu (1 - \gamma^5) f' W_\mu^+ + h.c.) + \mathcal{L}_{Z ff} = -\frac{g}{\cos \theta_W} \bar{f} \gamma^\mu (g_V^f - g_A^f \gamma^5) f Z_\mu + \mathcal{L}_{gqq} = -g_s \bar{q} \gamma^\mu T^a q G_\mu^a$$

$$+ \mathcal{L}_{\text{mass}} = M_W^2 W_\mu^+ W^{-\mu} + \frac{1}{2} M_Z^2 Z_\mu Z^\mu + \mathcal{L}_{\text{Yukawa}} = -y_d \bar{Q}_L \phi d_R - y_u \bar{Q}_L \tilde{\phi} u_R - y_e \bar{L}_L \phi e_R + h.c.$$

$$M_W = \frac{g \cancel{v}}{2}, \quad M_Z = \frac{g \cancel{v}}{2 \cos \theta_W}.$$

$$m_f = \frac{y_f \cancel{v}}{\sqrt{2}}.$$



$$V(\phi) = -\mu^2 \phi^\dagger \phi + \lambda (\phi^\dagger \phi)^2$$

and ϕ is a complex field doublet:

$$\phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix}$$

where we choose:

$$\mu^2 < 0 \text{ and } \lambda > 0$$

and

$$v^2 = \frac{-\mu^2}{\lambda}, \quad m_H^2 = 2\lambda v^2.$$

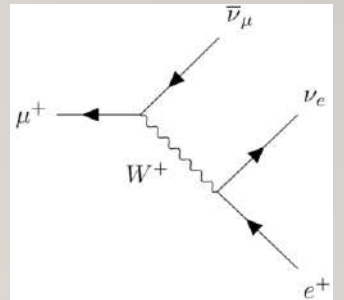
HIGGS VACUUM

1. Higgs potential is determined with 2 **free parameters** μ and λ , where:
 1. $m_H^2 = -2\mu^2$ (if $\mu^2 > 0$ symmetries of $\mathcal{L}$ remains unbroken)
 2. λ is the coupling strength of Higgs self-interaction (**self-coupling**)

2. Absolute minimum of the potential (vev) v can be derived from μ and λ and it contributes to the energy density of the Universe

3. v can be determined from the Fermi constant G_F measured in muon decay $G_F = 1/(v^2 \cdot \sqrt{2})$

$$v = 246.22 \text{ GeV.}$$

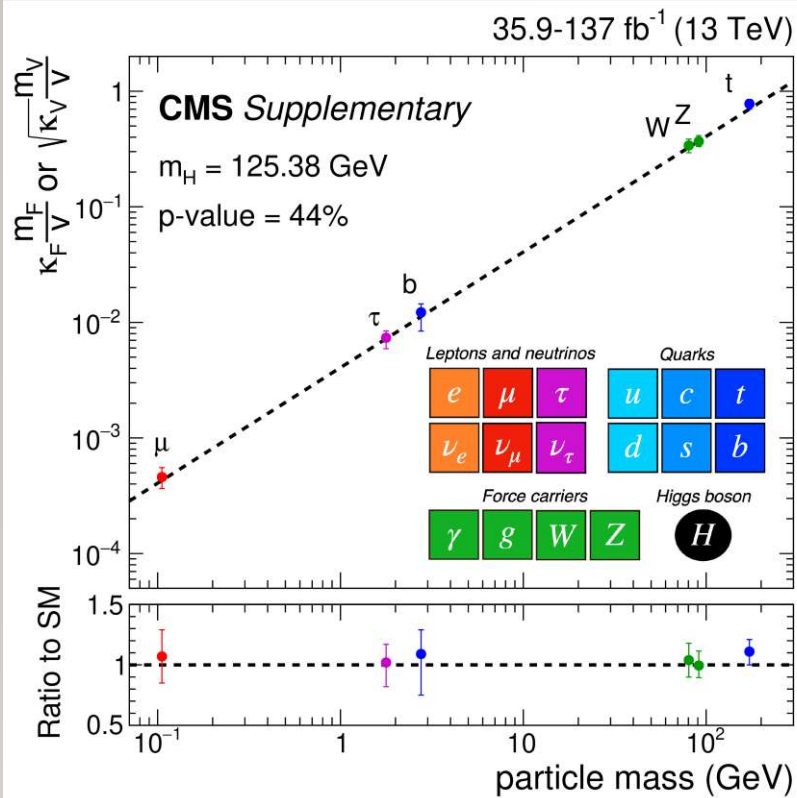


4. λ can be determined from the Higgs mass:

$$m_H = 125.25 \pm 0.17 \text{ GeV}$$

giving:

$$\lambda = 0.1291 \pm 0.0004$$



HIGGS COUPLINGS

1. Particles Yukawa couplings are linearly dependent on their masses:

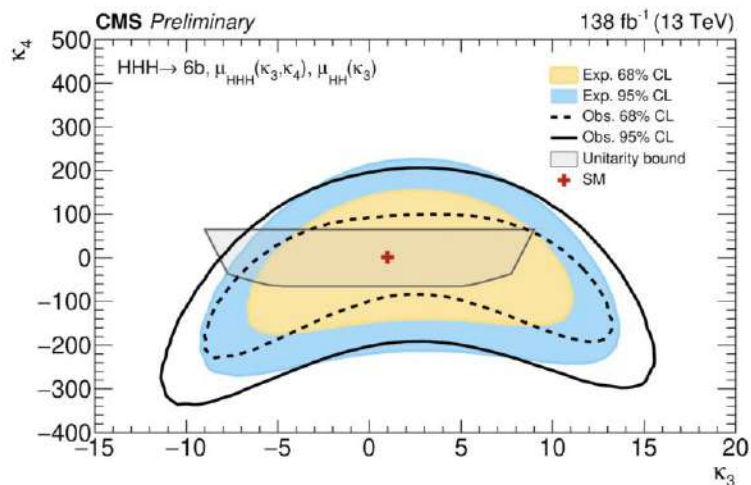
$$m_f = \frac{y_f v}{\sqrt{2}}.$$

2. Any deviation of the linearity will be a sign of new physics
3. Higgs self-coupling has to be directly measured

4. More precise the measurements – better sensitivity to new physics

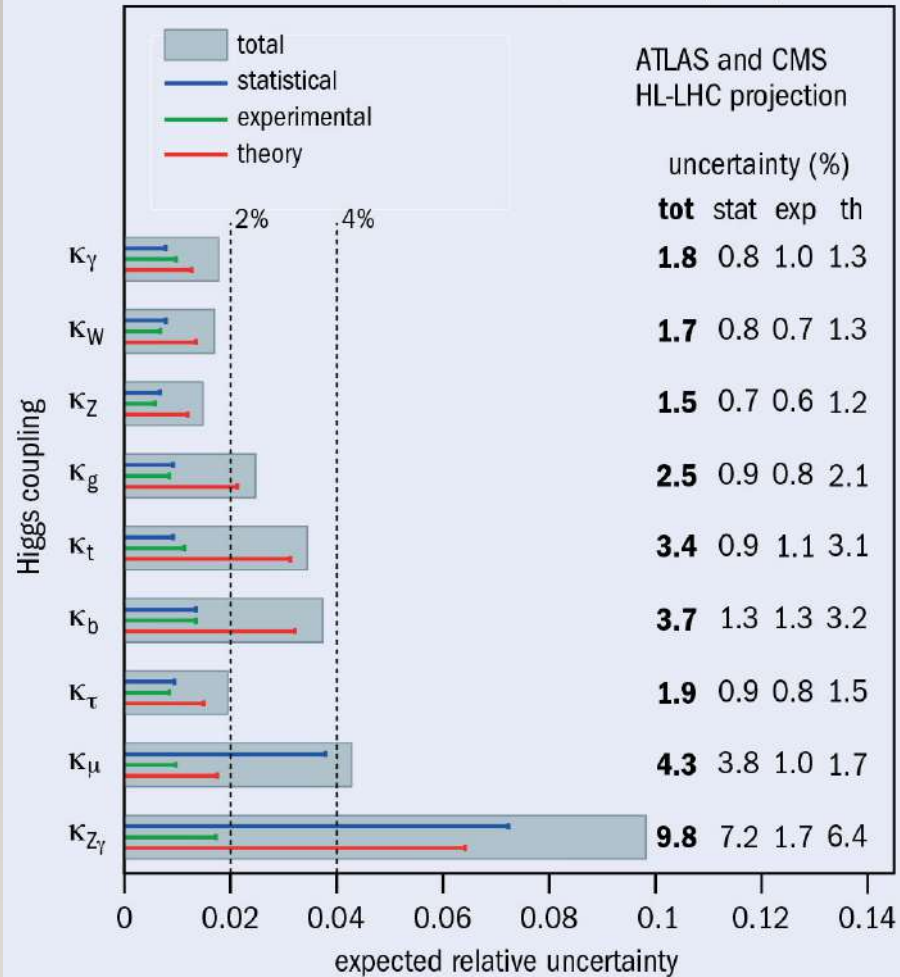
5. Current measurements gives relative uncertainties typically larger than (few times) 10%, while λ could deviate several times from the SM prediction.
6. HL-LHC full run should bring down relative uncertainty of λ to ~30%

7. Can Higgs couplings be measured better (more accurate) and how?



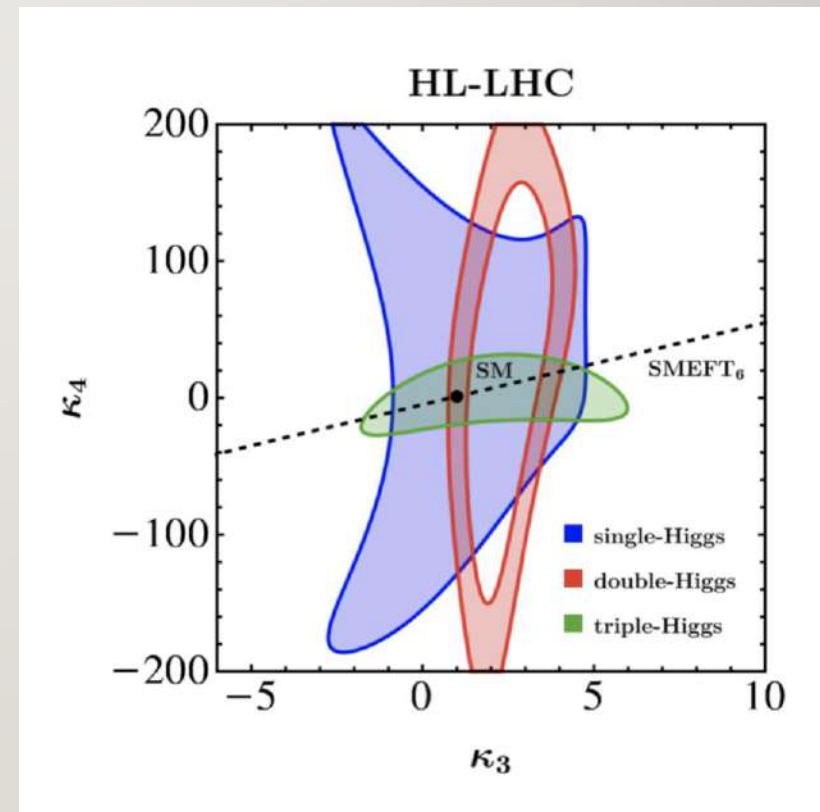
CAN HIGGS COUPLINGS BE BETTER MEASURED AND HOW?

$\sqrt{s} = 14 \text{ TeV}, 3000 \text{ fb}^{-1} \text{ per experiment}$

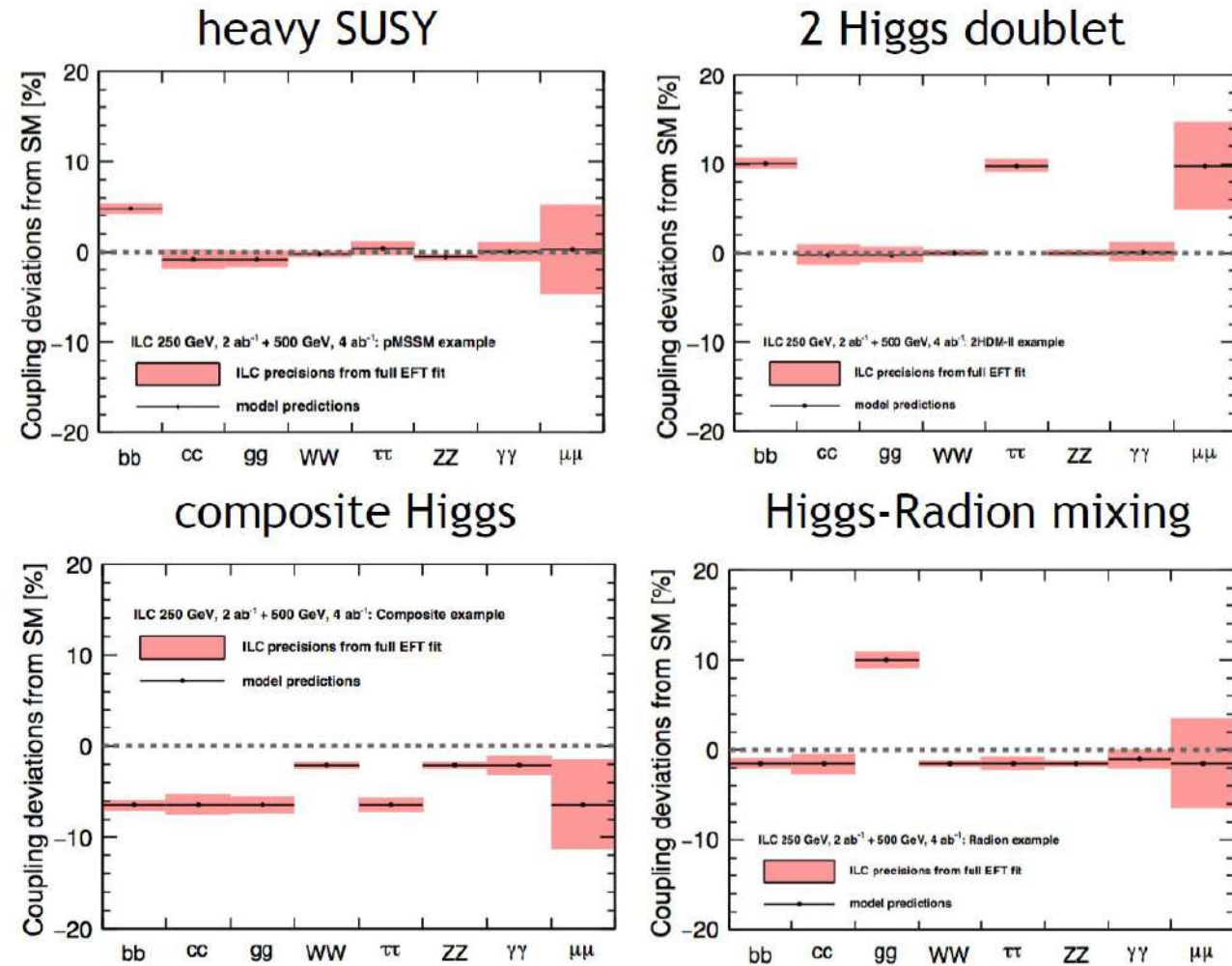


HL-LHC, 13 TeV, 3 ab^{-1} (~10 years, 2041)

a few percent (relative statistical precision) for Higgs couplings



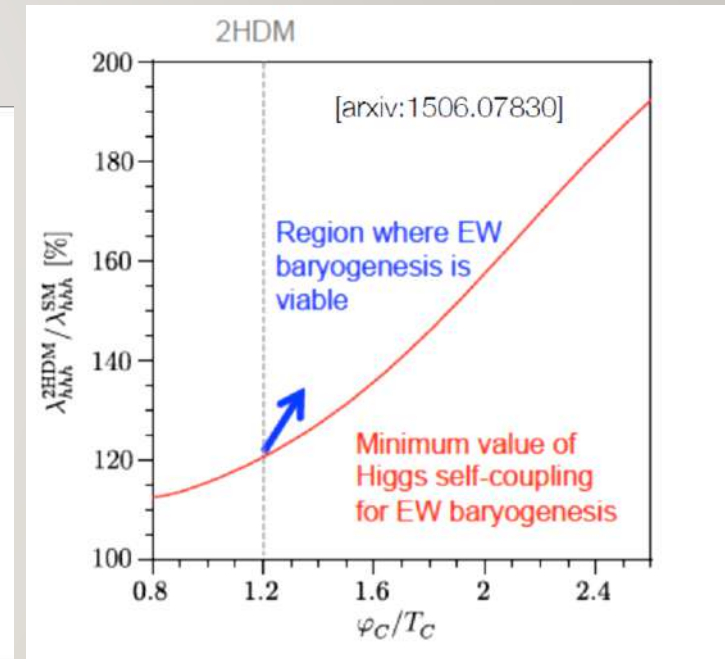
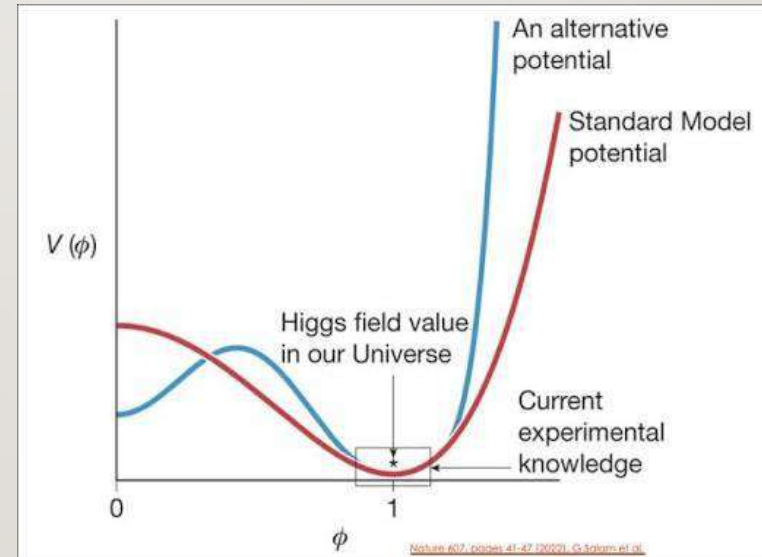
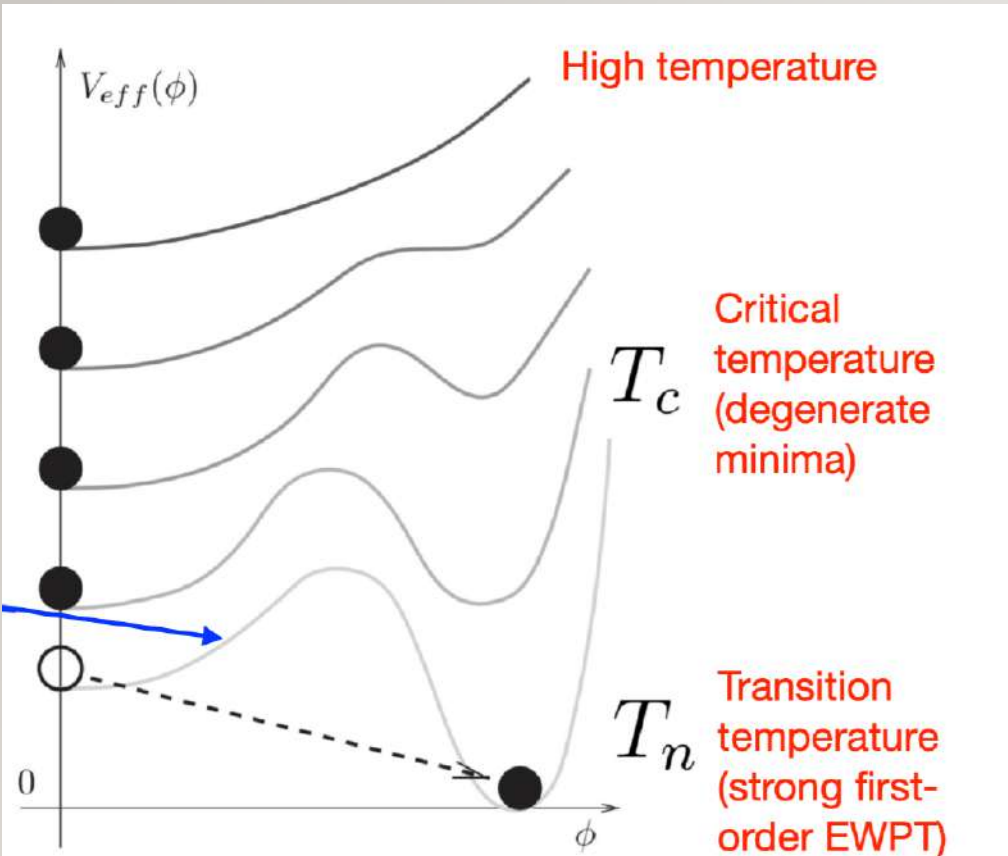
HOW PRECISE DO WE NEED HIGGS COUPLINGS?



- I. Depends on the model and coupling, but, in general, at a percent level or better

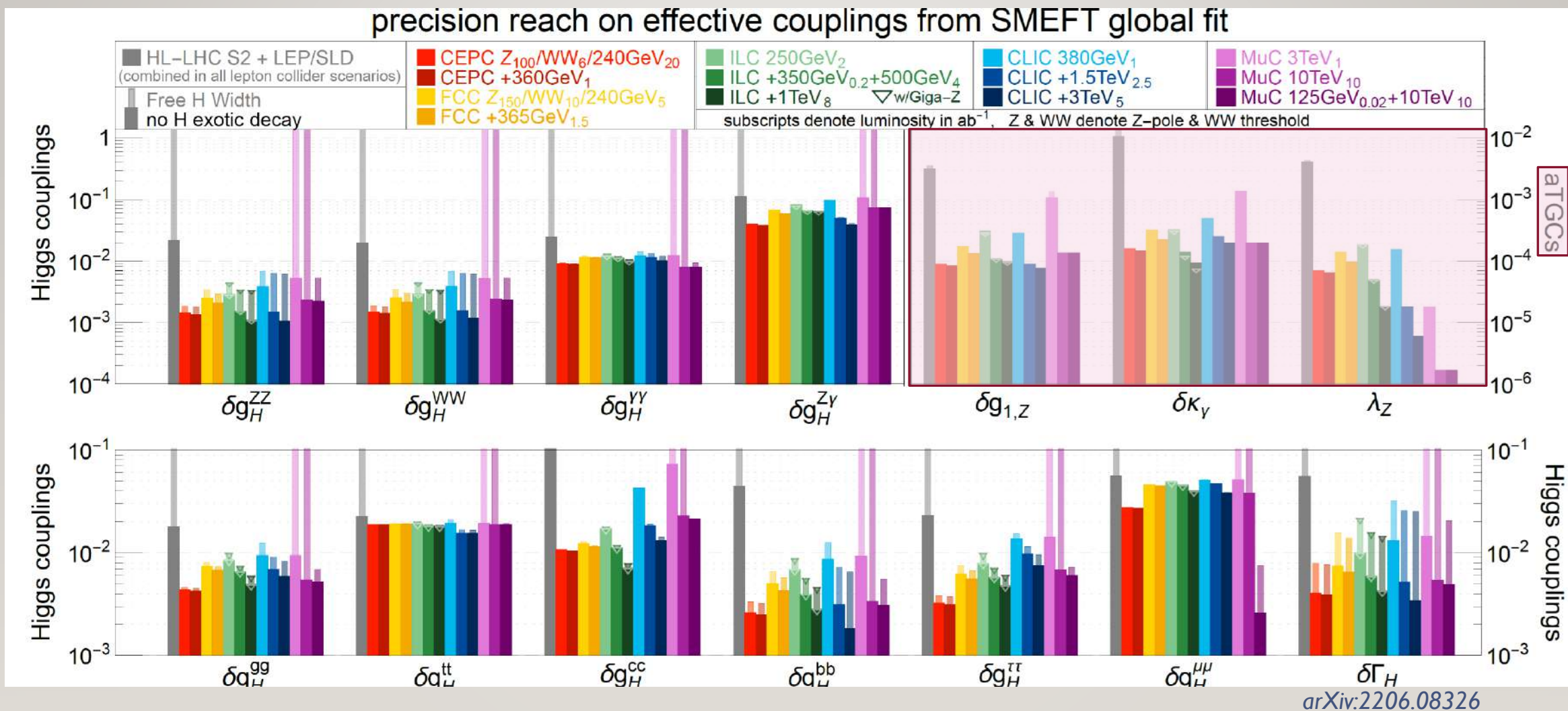
HIGGS SELF COUPLING

1. Which shape of the Higgs potential is realized in nature (is $\lambda = \lambda_{\text{SM}}$)?
2. Could Higgs be responsible for baryogenesis?
3. EW baryogenesis requires first-order phase transition (i.e. $\lambda > 1.2 \lambda_{\text{SM}}$)

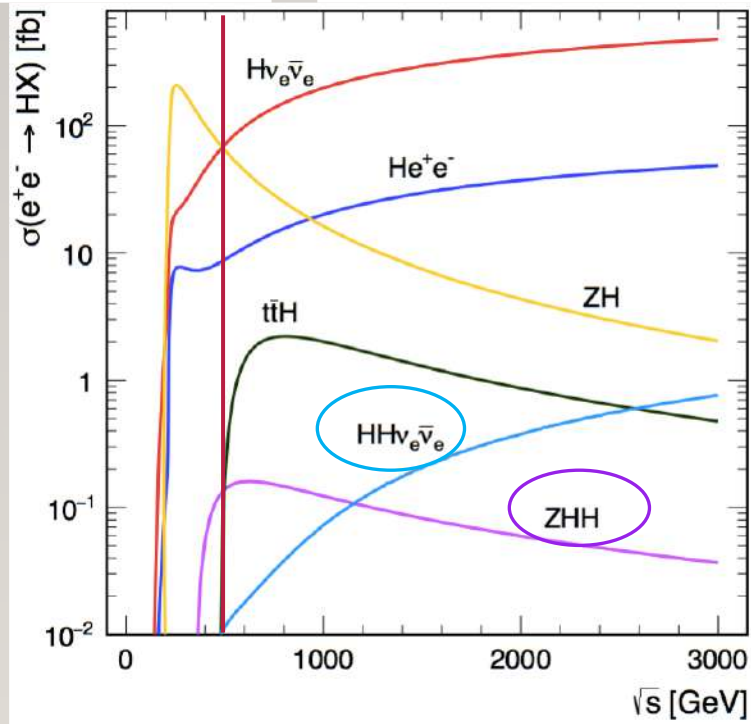
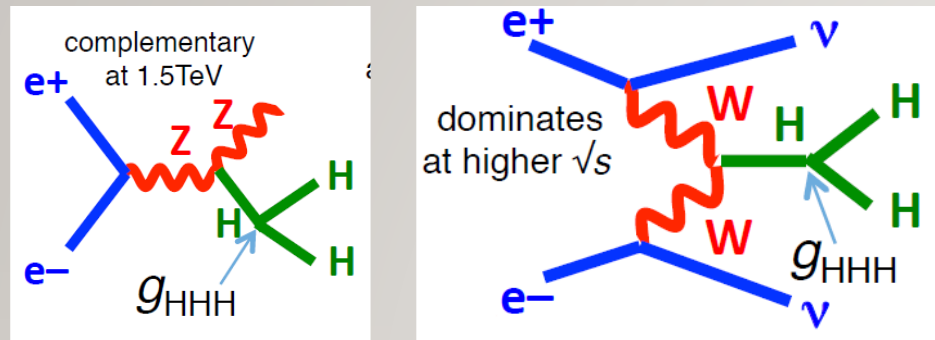


CAN WE MEASURE H.Cs BETTER (THAN AT HL-LHC)?

Yes, and for that e^+e^- (lepton) colliders are needed

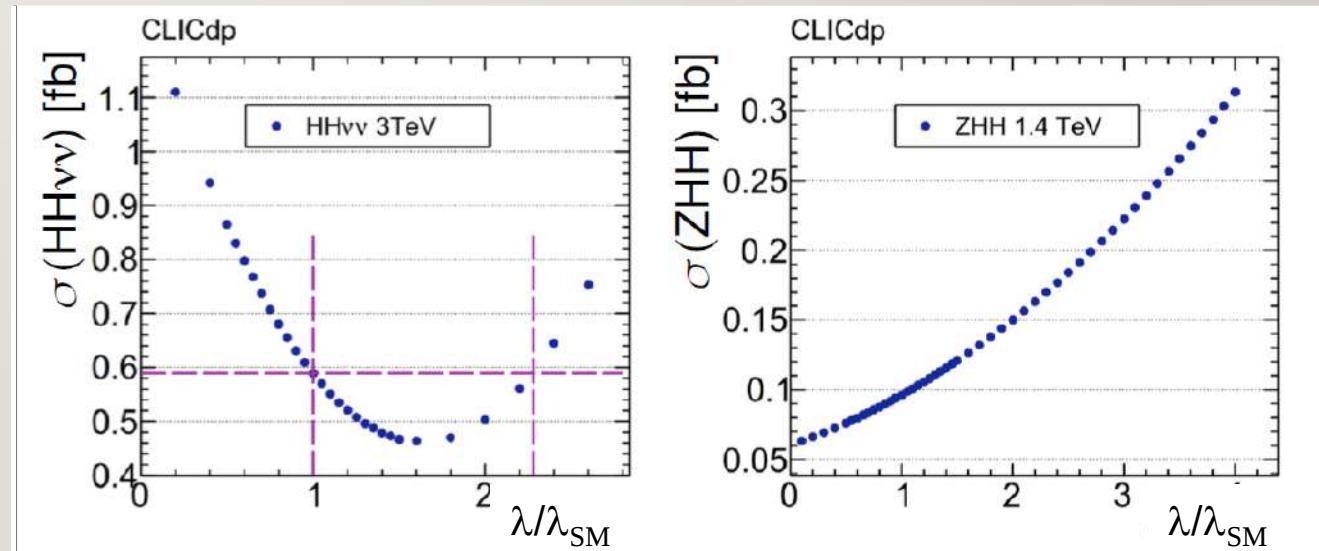


CAN WE MEASURE λ BETTER (THAN AT HL-LHC)?

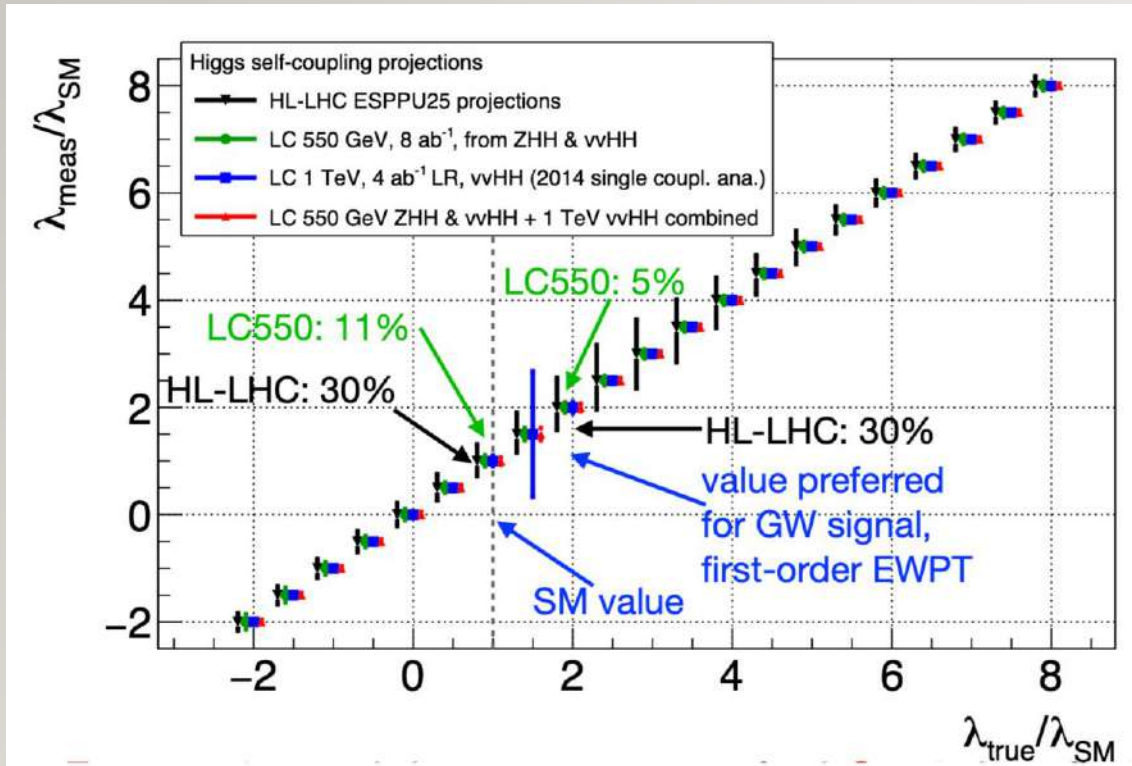


Yes, and for that e^+e^- (lepton) colliders are needed

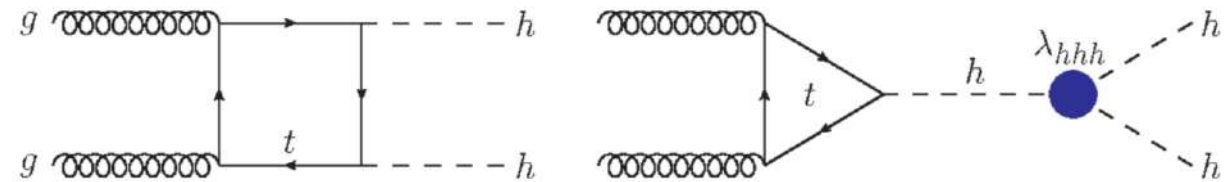
1. In particular those operating at and above 500 GeV
2. Because double Higgs production can be directly accessed (in WW -fusion)
3. In addition, one benefits from different $HH\nu\nu$ and ZHH cross-sections behavior w.r.t. λ

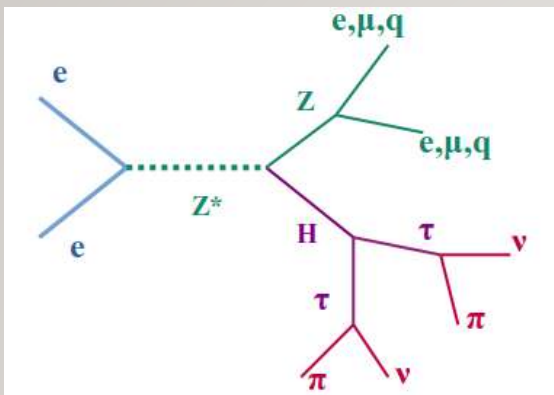


CAN WE MEASURE λ BETTER (THAN AT HL-LHC)?



1. Precision (relative) down to few percent, depending on λ
2. Significant gain w.r.t. HL-LHC
3. At hadron colliders destructive interference occurs between HH production channels
4. And that interference is larger for larger $\lambda/\lambda_{\text{SM}}$
5. To test EW baryogenesis one needs high-energy lepton collider(s)





HIGGS HAVE OTHER PROPERTIES: SPIN

1. SM Higgs is a pure scalar $J^P = 0^+$
2. It has to be tested
3. Could 125 GeV mass eigenstate of a mixture of scalar and pseudoscalar?

$$h_{125} = H \cdot \cos(\psi_{CP}) + A \cdot \sin(\psi_{CP})$$

4. In that case CP symmetry is violated (maximally for $\Psi_{CP} = \pi/4$)
5. Higgs interactions (both production and decays) could provide CP violation - Saharov's condition (one of) for baryogenesis
6. Current ATLAS/CMS precision 279 mrad
7. HL-LHC (3 ab^{-1}) $\sim 90 \text{ mrad}$

Future colliders	Energy	Integrated luminosity	$\Delta\Psi_{CP}$ (68% CL)
ILC250	250 GeV	2 ab^{-1}	75 mrad
FCC-ee240	240 GeV	10.8 ab^{-1}	44 mrad
CEPC240	240 GeV	5.6 ab^{-1}	16 mrad

HIGGS INTERACTS WITH ANY MASSIVE PARTICLE

HADRON COLLIDERS

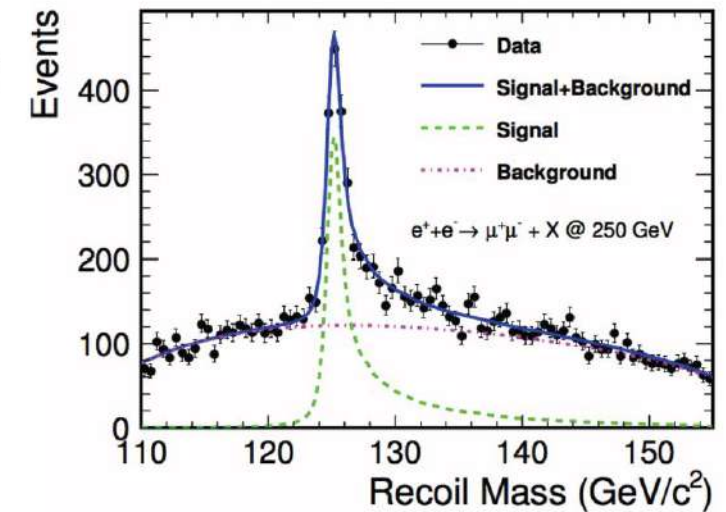
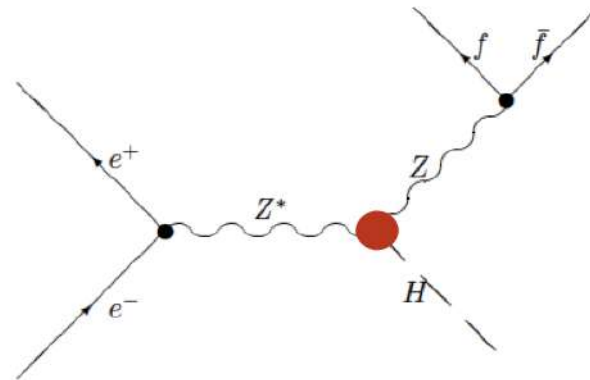
- No absolute measurement of the production cross-section (like ZH at e⁺e⁻ colliders)
- Higgs couplings come in combination:
$$\sigma(H) \times \text{BR}(H \rightarrow a + b) \sim \frac{\Gamma_{\text{prod}} \Gamma_{\text{decay}}}{\Gamma_{\text{tot}}}$$
- Only ratio of couplings can be directly determined (i.e. $g_{H\tau\tau}^2/g_{HWW}^2$)

LEPTON COLLIDERS

- Absolute measurement of the ZH cross-section
- Absolute measurement of the Higgs BRs
- Nearly model-independent determination of the Higgs total width and couplings

1. Higgs interactions (total width) includes yet undiscovered particles, invisible particles, Dark Matter particles (WIMP), etc.
2. These are additional reasons (to coupling mass linearity) why Higgs BR fractions have to be precisely measured (in particular Higgs to invisible)

$$M_{\text{recoil}}^2 = s + M_Z^2 - 2\sqrt{s} E_Z$$

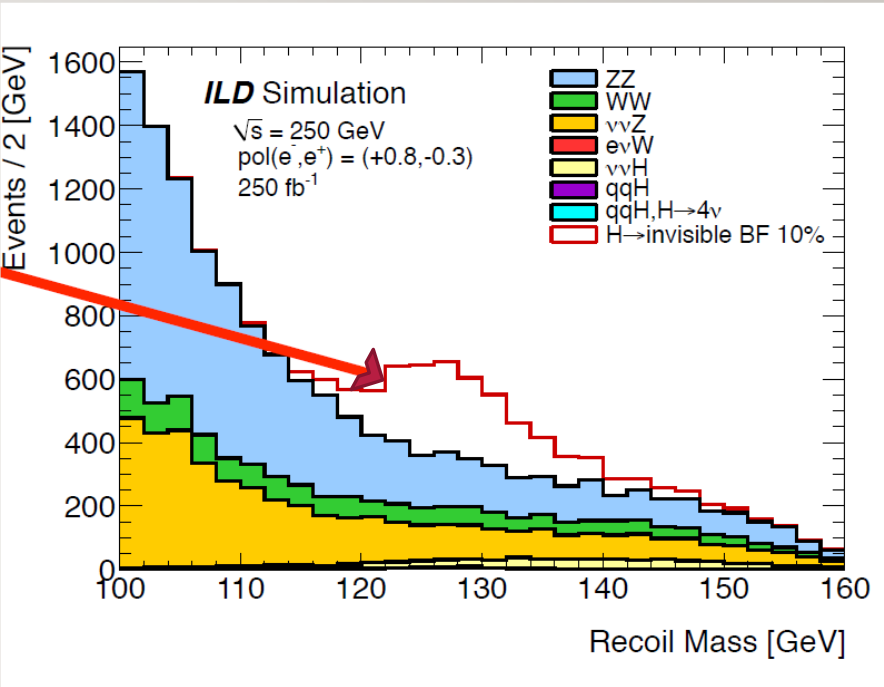


HIGGS INVISIBLE DECAYS AT LEPTON COLLIDERS

FCCee 240GeV

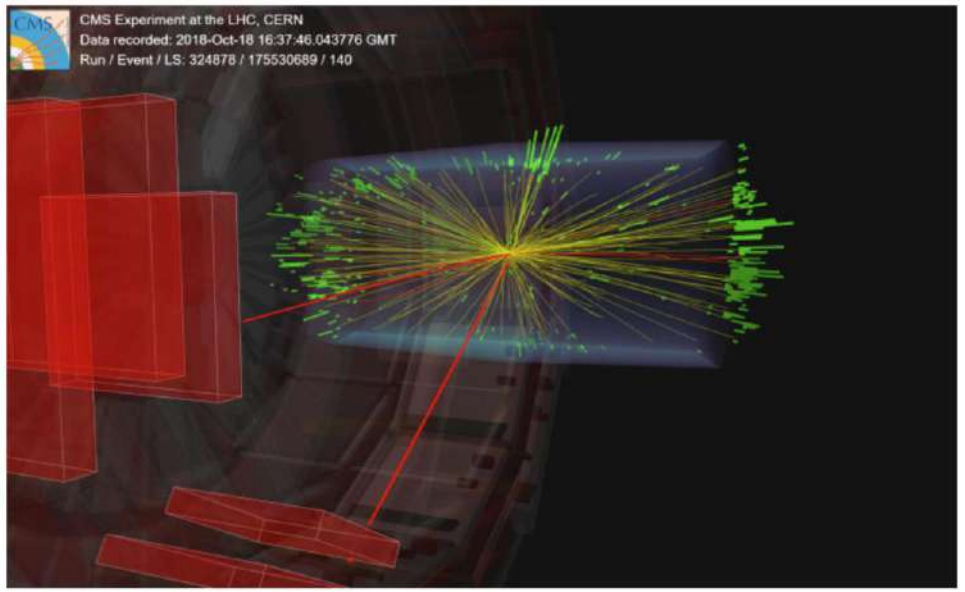
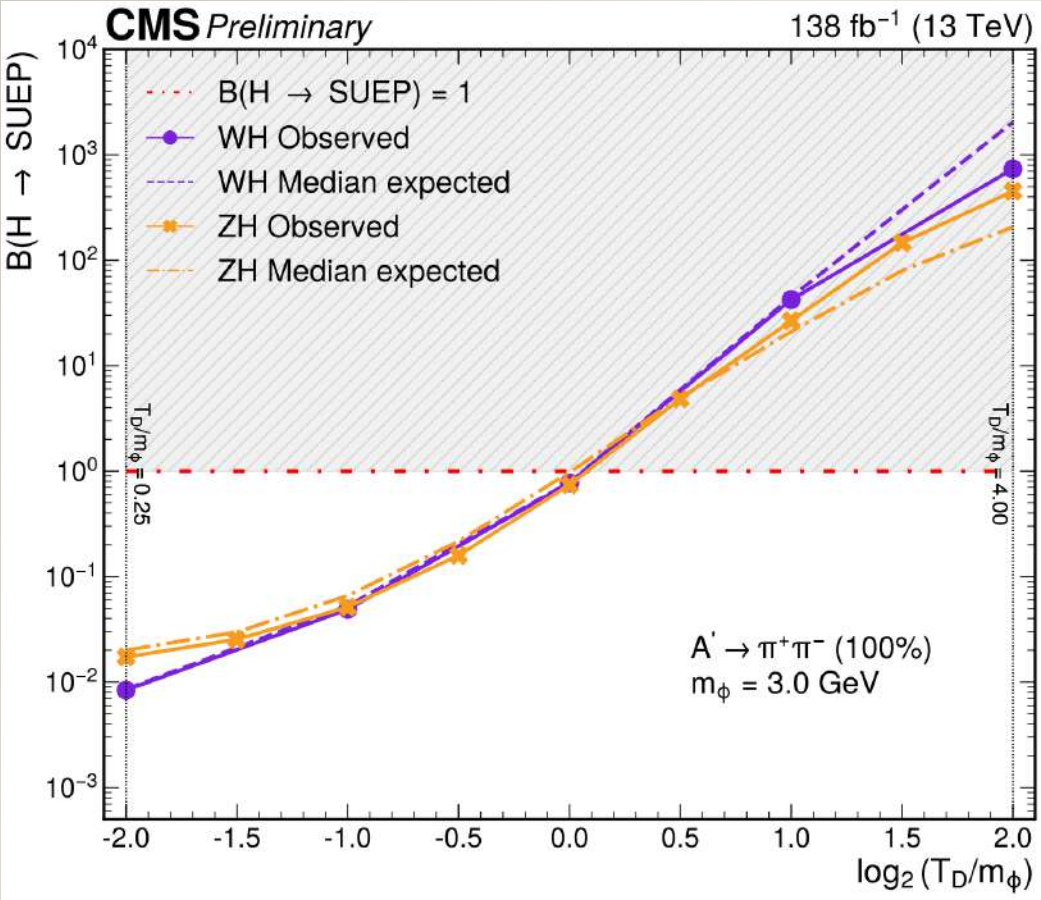
Expected 95% CL upper limits on the branching fraction for the ee , $\mu\mu$, and qq channels.

Physics	Upper Limit on $\mathcal{B}(H \rightarrow inv.)$
$Z(ee)H(inv)$	0.43%
$Z(\mu\mu)H(inv)$	0.35%
$Z(qq)H(inv)$	0.15%
Combined	0.15%

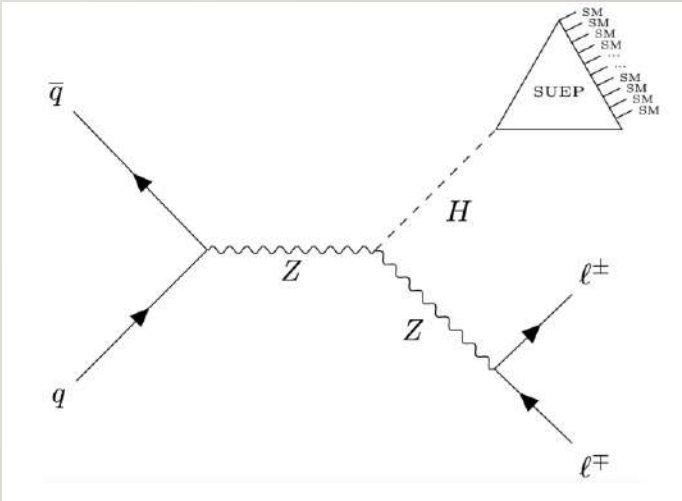


ILC 250GeV 95% CL (0.16-0.3)%

HIGGS INVISIBLE DECAYS AT LHC



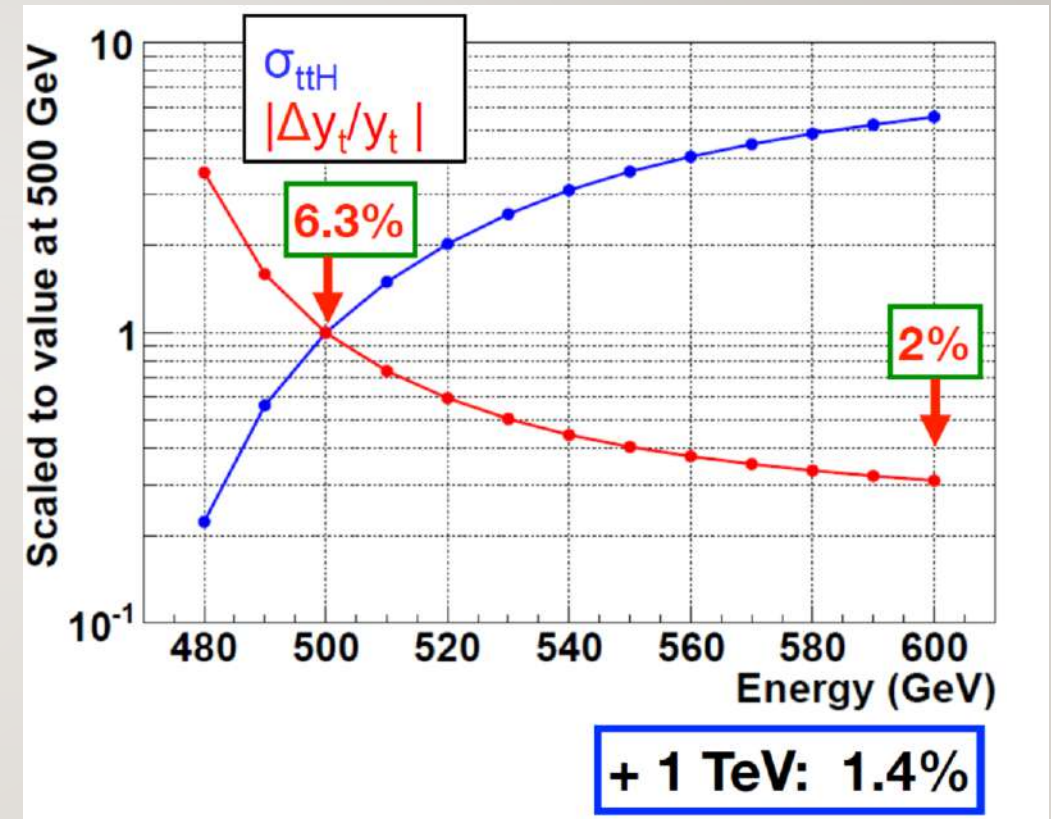
Soft Unclustered Energy Pattern (SUEP)



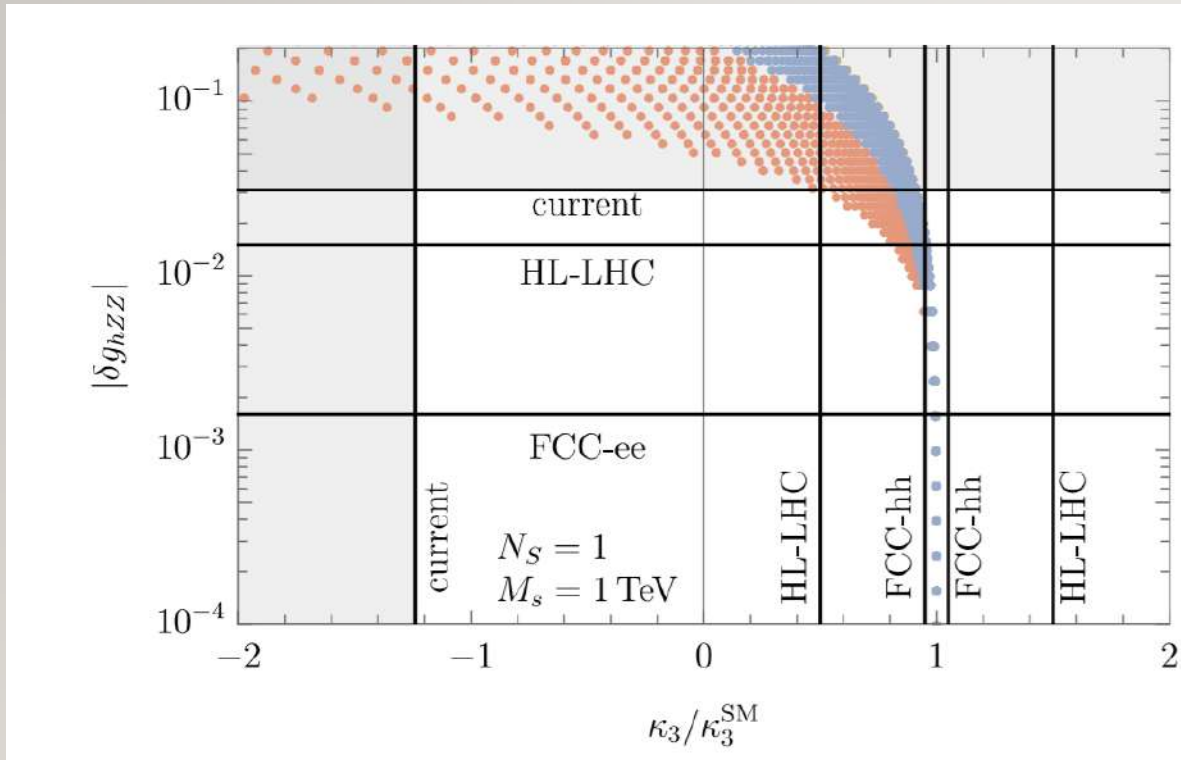
t-QUARK: HIGGS STRONGEST COUPLING

1. CP can be violated in ttH production (Higgs is too heavy to decay to top pair)
2. High energy lepton colliders are crucial for both CPV and top-Yukawa coupling y_t measurement
3. Reaching theoretical target ($f_{CP} \sim 10^{-2}$ for Higgs-fermion vertices) at 1 TeV
4. f_{CP} = fraction of the CP-odd contribution to the total interaction rate

$f_{CP} \cdot 10^{-2}$	500 TeV e^+e^- 0.5 ab^{-1}	1 TeV e^+e^- 1 ab^{-1}
	29	8



HIGGS AND VACUUM STABILITY

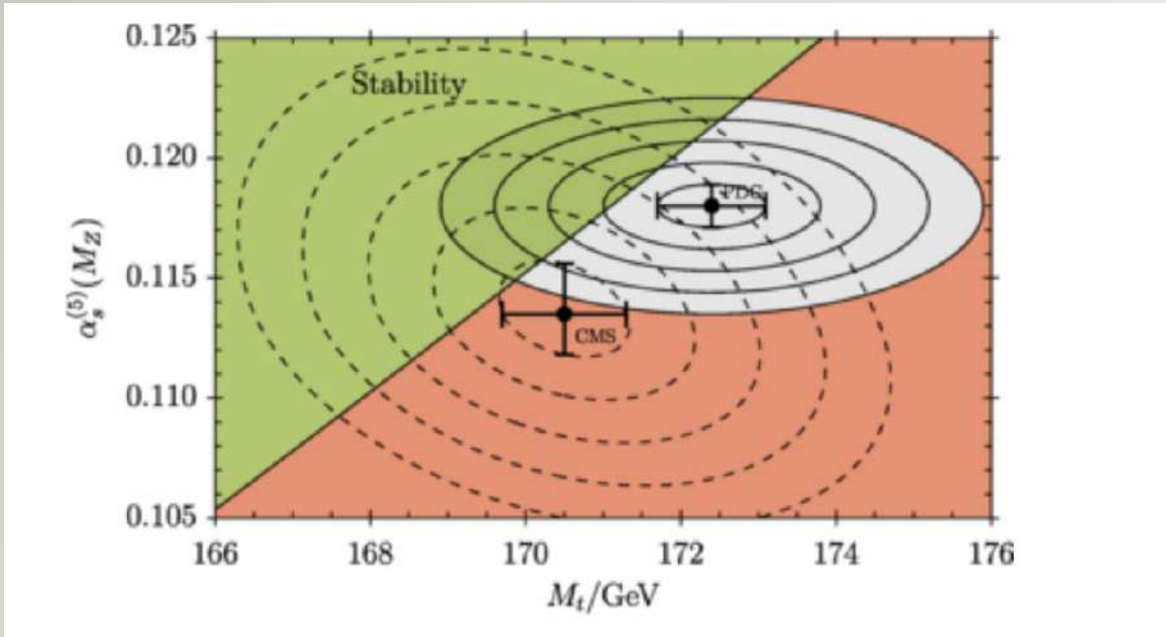


1. We are still not (sufficiently) sure if Higgs is SM (dots correspond to various BSM realizations of Higgs)
2. We don't know Higgs coupling sufficiently precise
3. We don't know Higgs self coupling with sufficient precision
4. Sufficient = is relativistic vacuum stable (blue) or not (red)

1. New experiments are needed
2. Different ones suitable to different $\lambda(\kappa_3)$
i.e. linear colliders for $\lambda > \lambda_{\text{SM}}$

<https://arxiv.org/pdf/2401.08811>

HIGGS (top) AND VACUUM STABILITY



1. Understanding the vacuum stability also requires t-quark mass (Yukawa coupling) precision
2. Metastable vacuum (within 1σ) – current
3. About 0.1–0.3% precision on the top Yukawa coupling would be needed to make a 5σ statement about whether the electroweak vacuum is truly metastable assuming the Standard Model is valid up to the Planck scale
4. Full FCC program (FCCee+FCChh) $\sim 1\%$ on y_t

HIGGS AND INFLATION

Think of a rubber sheet.

- The sheet = spacetime geometry.
- Curvature of the sheet = R .
- A heavy object deforming the sheet = energy density.

The usual Einstein theory says:

Energy bends the sheet.

Higgs inflation adds:

The amount by which the sheet bends depends also on the local Higgs field value.

1. Higgs field potential is at these energies (10^{16-17} GeV) controlled by quartic coupling λ_4
2. And λ_4 running (with energy scale μ) goes like:

$$d\lambda_4/d(\ln \mu) \sim -6 y_t^4$$

1. Again, Higgs self-couplings are crucial to understand its connection to the Universe
2. As well as top Yukawa coupling

The Higgs quartic coupling λ_4 is not directly measured at any collider. What colliders measure is mainly the Higgs self-coupling (trilinear coupling λ_3) through double-Higgs production. The quartic term in the potential is

$$V(H) = -m^2 H^\dagger H + \lambda_4 (H^\dagger H)^2,$$

and after electroweak symmetry breaking it gives

$$\lambda_3 = \lambda_4 v,$$

(up to conventional factors). Therefore, the experimental precision usually quoted is:

$$\frac{\Delta \lambda_3}{\lambda_3}$$

and this translates into a precision on λ_4 of essentially the same relative size.

HOW FAR CAN WE GO IN PRECISION?

1. The goal is not comparison – it's the order of magnitude



2. Different assumptions and level of details

3. But, this is what we approximately can hope for

4. Two critical measurements require high energy (linear lepton or circular hadron) collider

Higgs observable	CIRCULAR LEPTON (FCC-ee)	LINEAR LEPTON (ILC)
Inclusive $\sigma(\text{ZH})$	0.17%	$\sim 0.30\text{--}0.35\%$
Higgs mass	≈ 5 MeV	$\approx 14\text{--}20$ MeV
Total width Γ_{H}	$\approx 1.1\%$	$\approx 1.8\text{--}2.0\%$
(g_{HZZ})	0.16%	$\approx 0.25\text{--}0.30\%$
(g_{HWW})	0.40%	$\approx 0.5\%$
(g_{Hbb})	0.56%	$\approx 0.7\text{--}0.8\%$
(g_{Hcc})	$\approx 1.2\%$	$\approx 1.5\text{--}1.8\%$
(g_{Hgg})	$\approx 0.9\%$	$\approx 1.0\text{--}1.2\%$
$(g_{\text{H}\tau\tau})$	$\approx 0.6\text{--}0.7\%$	$\approx 0.8\text{--}0.9\%$
$(g_{\text{H}\mu\mu})$	$\approx 4\%$	$\approx 5\text{--}6\%$
$(g_{\text{H}\gamma\gamma})$	$\approx 1.3\%$	$\approx 2\%$
(g_{Htt})	— (no direct measurement)	$\approx 1.4\%$
Higgs self-coupling (SM)	— (no direct measurement) $\approx 40\%$ (indirect)	$< 10\%$
$\text{BR}(\text{H} \rightarrow \text{invisible})$ 95% CL	$< 0.2\%$	$\approx 0.16\text{--}0.3\%$
CP mixing angle $(\text{H} \rightarrow \tau\tau)$	44 mrad	75 mrad

CURRENT VISDOM

1. Higgs boson plays a major role in mass generation
2. It is responsible for properties of the Universe:
 1. Vacuum energy
 2. Vacuum stability
3. It may be responsible for many others:
 1. EW baryogenesis
 2. Baryon asymmetry
 3. Cosmological inflation (Bezrukov and Shaposhnikov, 2008)
4. It interacts with any massive particle (including yet unknown)
 1. Invisible and exotic decays
 2. Dark Matter

- Katarina Anthony

CURRENT VISDOM

A Cosmic Microwave Background (CMB) fluctuation map showing temperature variations across the sky. A red line is drawn across the map, and a diagram of a satellite orbit is visible in the upper right corner.

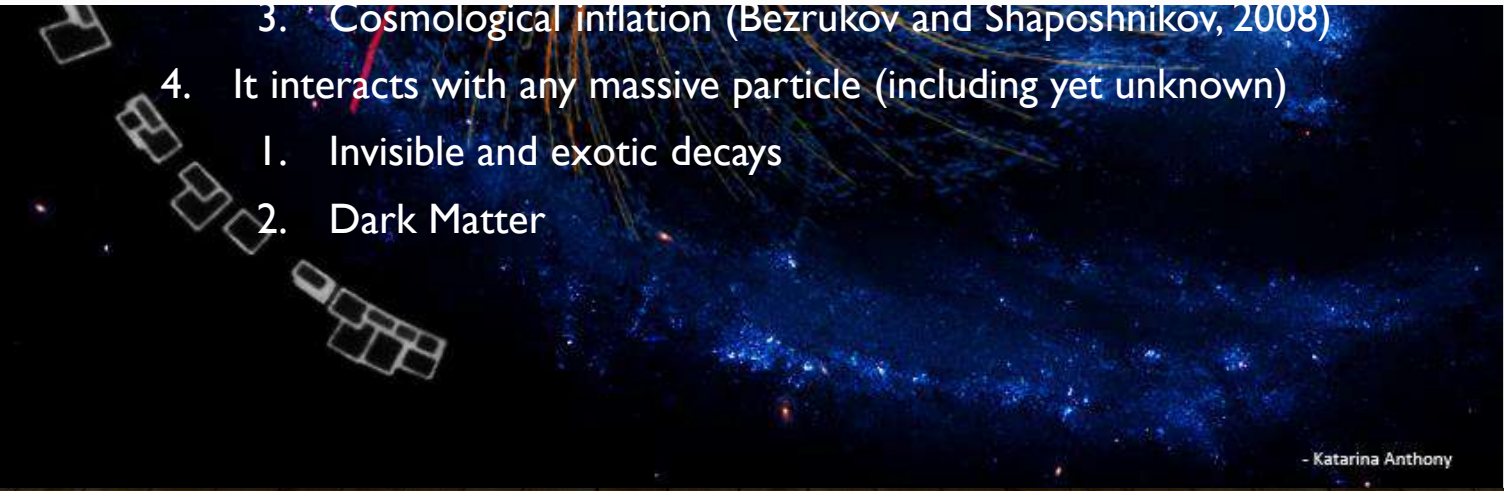
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The Higgs mass tells us where we start.

The top Yukawa tells us which direction the Higgs potential flows.

The Higgs self-coupling tells us whether the potential itself has the Standard Model shape.

Gravity asks what happens when the Higgs field is pushed to the largest possible values.

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To probe Higgs relation to the Universe
high energy colliders are needed:
lepton (e^+e^-) linear @TeV or hadron circular @ 10^2 TeV

- Katarina Anthony

HIGGS BOSON: HOW TO MEASURE IT?

WHAT IS ON THE TABLE: e^+e^- COLLIDERS AND THEIR EXTENSIONS

WHAT IS ON THE TABLE?

	Collider	Size (km)	$\sqrt{s}$ (GeV)	IPs	Beam polarization	Peak luminosity / IP ($10^{34} \text{ cm}^{-2} \text{ s}^{-1}$)	Integrated luminosity (machine)	Integrated luminosity / detector	Higgs bosons / detector	Nominal run time
C I R C U L A R	LEP3	27	240	2	No	~1	1.0 ab^{-1}	0.5 ab^{-1}	~100,000	~5 yr
	CEPC	100	240	2	No	3.0	11.2 ab^{-1}	5.6 ab^{-1}	~1.1 million	~7 yr
	FCC-ee	91	240	4	No	8.5	10.8 ab^{-1}	2.7 ab^{-1}	~500,000	~3 yr
	FCC-ee	91	365	4	No	1.7	2.7 ab^{-1}	0.675 ab^{-1}	~250,000	~4 yr
	LCF	33	380	1	$\pm 80\% \text{ e}^-$, $\pm 30\% \text{ e}^+$	2.7	1.0 ab^{-1}	1.0 ab^{-1}	~350,000	~8 yr
L I N E A R	ILC	21	250	1 (2 with dual BDS)	$\pm 80\% \text{ e}^-$, $\pm 30\% \text{ e}^+$	~1.35	2.0 ab^{-1}	2.0 (or 1.0 with 2 IPs)	~500,000 (250k/IP with 2 IPs)	~11–12 yr
	ILC	31	550	1 (2 with dual BDS)	$\pm 80\% \text{ e}^-$, $\pm 30\% \text{ e}^+$	~1.8	~4.0 ab^{-1} (under discussion)	4.0 (or 2.0)	~1 million	~8 yr
	ILC	48	1000	1 (2 with dual BDS)	$\pm 80\% \text{ e}^-$, ± 20 – 30% e^+	~4.9	8.0 ab^{-1}	8.0 (or 4.0)	~2.5 million	~10 yr

WHAT IS ON THE TABLE?

proposed by CERN

possibly considered by CERN

possibly proposed by China

possibly considered by CERN

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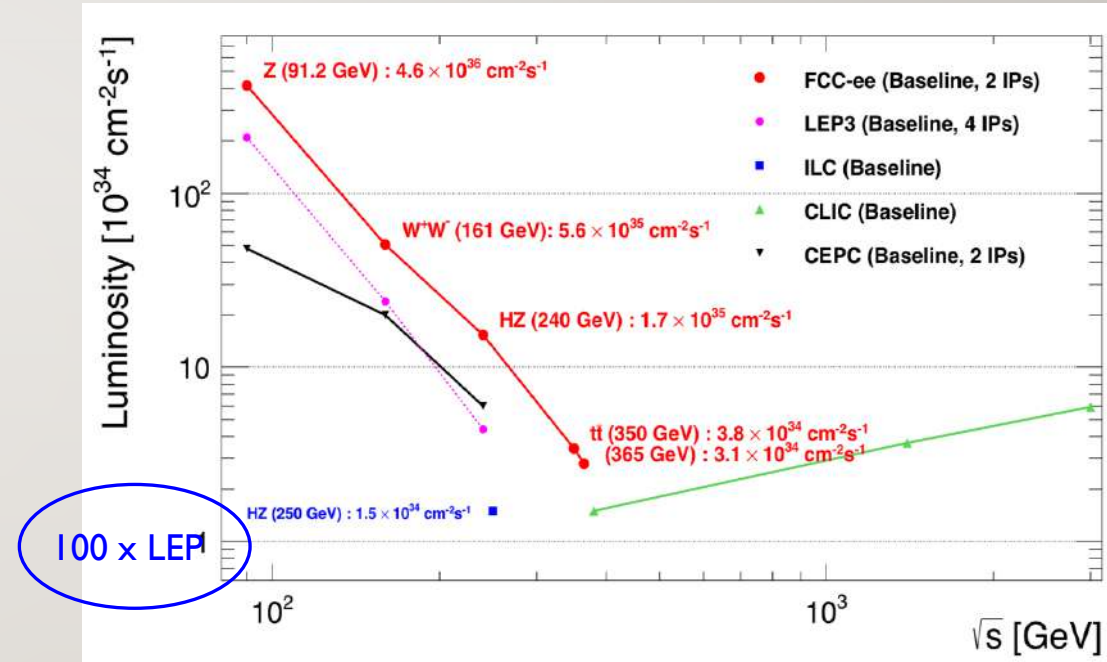
UNDERSTANDING THE TABLE

CIRCULAR

1. It seems that there is a preference towards circular machines
2. Beam is reusable, multiply integrated luminosity with number of IPs
3. Initially used leptons can be replaced by hadrons (pp): FCCee $\rightarrow$ FCChh and CEPC $\rightarrow$ SPPC

LINEAR

1. Instantaneous luminosity can not compare (to circular)
2. But, beams can be polarized
3. Straightforward (literally) in length to higher energies where offer unique precision for λ and y_t



WHAT IS IN COMMON FOR FUTURE LEPTON COLLIDERS?

TECHNICAL DIFFERENCES ARE NUMEROUS, BUT

1. Based on SC RF technology ('cold' machines)
2. Know initial state → final state reconstructable from the first principles
3. Absolute normalization of the Higgs couplings (σ_{HZ} measurement based on recoil mass)
4. All require precise tracking, high granularity calorimeters and a hermetic detector
5. Particle flow paradigm in particle reconstruction



Detector studies are common and transferable

PRINCIPAL DIFFERENCES ARE DETERMINED BY SHAPE

1. Large synchrotron radiation at circular colliders → heavier particles and/or larger radius

$$U_0 \propto \frac{E^4}{m^4 \rho}.$$

2. Very difficult to polarize circular beams - repeated bending in magnetic fields causes the particle spins to undergo billions of precessions, making them highly sensitive to depolarization (from synchrotron oscillations, beam-beam effects)
3. Circular have larger instantaneous luminosities due to high repetition rate f (i.e. 30 times more collisions per second at FCC240 than ILC250)

$$L = \frac{N_b N^2 f}{4\pi \sigma_x \sigma_y},$$

THE FUTURE MUST BE ~~BRIGHT~~ PRECISE

nonexistent technology

Higgs observable	FCC-hh (100 TeV)	SPPC (75–125 TeV)*	ILC (250+550+1000)	CLIC (380+1.5+3 TeV)	Muon Collider (10 TeV)
g_{HZZ}	~1%	~1%	0.25–0.30%	~0.3%	~0.4%
g_{HWW}	~1%	~1%	0.5%	~0.5%	~0.5%
g_{Hbb}	~1%	~1%	0.7–0.8%	~0.7%	~0.5–0.7%
g_{Hcc}	~2–3%	~2–3%	1.5–1.8%	~1.5%	~1–2%
g_{Hgg}	~1–2%	~1–2%	1.0–1.2%	~1%	~1%
$g_{H\tau\tau}$	~1%	~1%	0.8–0.9%	~0.8%	~0.6–0.8%
$g_{H\mu\mu}$	~2–3%	~2–3%	~5%	~4%	≈1%
Top Yukawa g_{Htt}	1.5–2%	~1–2%	1.5–2% (550 GeV + 1 TeV)	≈2%	≈1%
Higgs self-coupling λ_3	3–5%	≈3–5%	≈10%	≈5–7%	≈2–4%

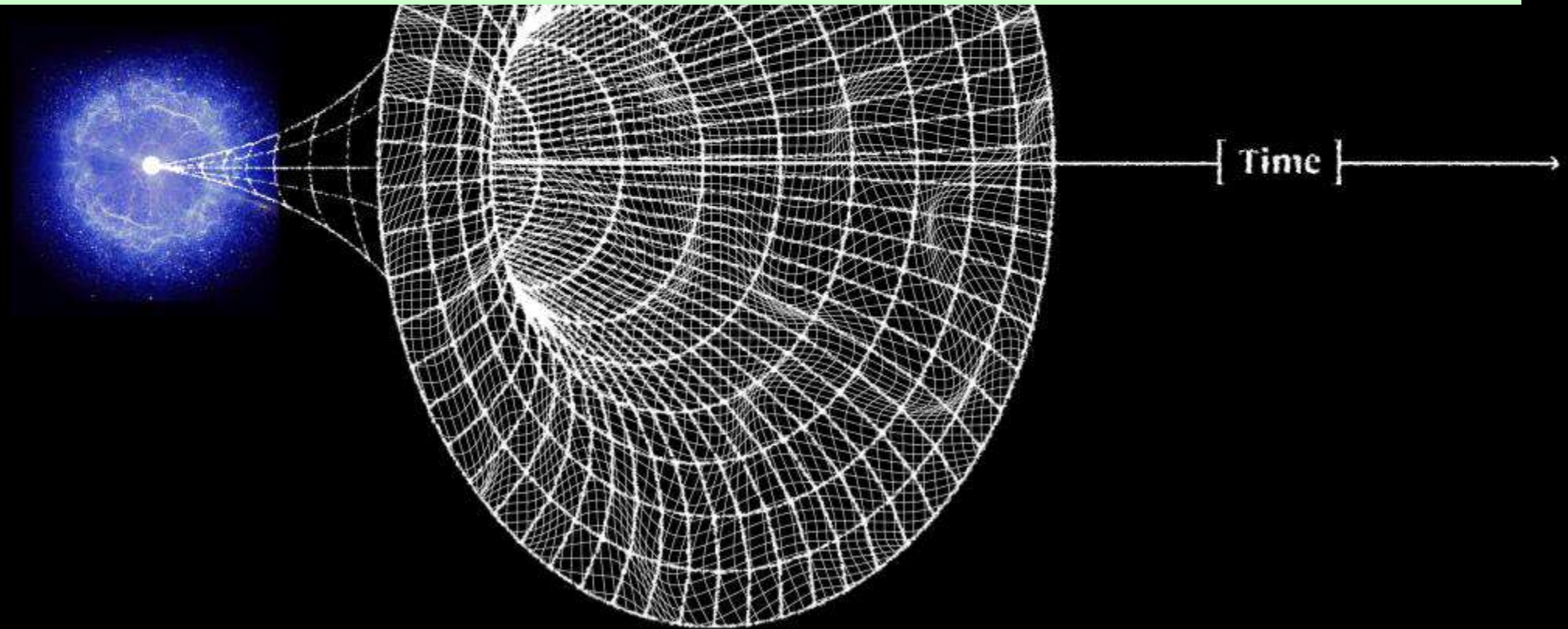
Collider project	Estimated construction cost	Comments	AI estimates
LEP3 Limited upgradability (inst. luminosity only)	≈7–10 BCHF	Never fully costed; estimate based on reuse of LHC tunnel and new RF system.	
CEPC (240 GeV)	≈5–6 BUSD	Includes 100 km tunnel and collider; significantly lower construction costs in China are assumed.	
FCC-ee Upgradable	≈10.8–11 BCHF	Latest FCC Feasibility Study estimate (2024 CHF), including tunnel, infrastructure, accelerator and CERN contribution to experiments.  Springer +1	
FCC-hh (incremental after FCC-ee)	≈16 BCHF	Reuses the FCC tunnel and much of the infrastructure. Dominated by the 14 T magnet system.  Springer	
FCC integrated programme (FCC-ee + FCC-hh)	≈27 BCHF	Staged investment over several decades (construction costs only, excluding long-term operating costs and most personnel).  Springer	
ILC250	≈6.5–7 BUSD	Official estimate for the first stage.	
ILC250→550→1000 GeV (Integrated program)	≈11–13 BUSD	Approximate total after staged upgrades; no single official number exists because the upgrades would be approved separately.	
LCF (250–550 GeV) Should be significantly less than 10 BUSD Upgradable	Not yet published	No official cost estimate has been released; expected to depend strongly on the maturity and industrialization of the high-gradient SRF technology.  IJCLab Events Di...	

SUMMARY

1. Higgs boson plays a vital role in our understanding of the Universe (vacuum energy, vacuum stability, EW baryogenesis, baryon asymmetry, cosmological inflation)
2. Higgs properties (BRs, CP properties) provide key relations to BSM
3. Higgs self interaction (in particular λ) and top Yukawa coupling y_t are crucial to provide the understanding of the relativistic vacuum and cosmological evolution including baryogenesis
4. To gain the knowledge of the above, high energy interactions are needed and can be provided by a linear collider at a TeV scale or circular pp colliders at hundred of TeV

1. But, the problem is that they are not easily affordable...
2. So, one look for the staged options (extendible physics program)
3. Where the question if the world can afford even the first stage is still open

It is surprising that measurements in the Higgs sector made at TeV scale can enhance our understanding of physics at 10^{16} GeV in the smallest fraction of the first second of the Universe.



СПАСИБО!



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